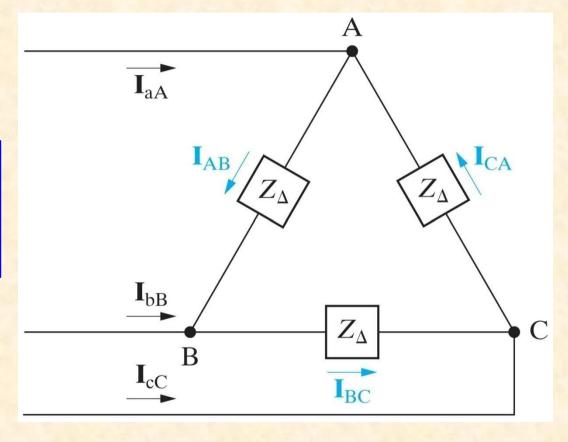
Balanced A-connected Load

✓ line voltages equal to phase voltages

$$V_L = V_{\phi}$$







Balanced A-connected Load

$$I_{AB} = \frac{V_{AB}}{Z_{\Delta}}$$

$$I_{BC} = \frac{V_{BC}}{Z_{\Delta}}$$

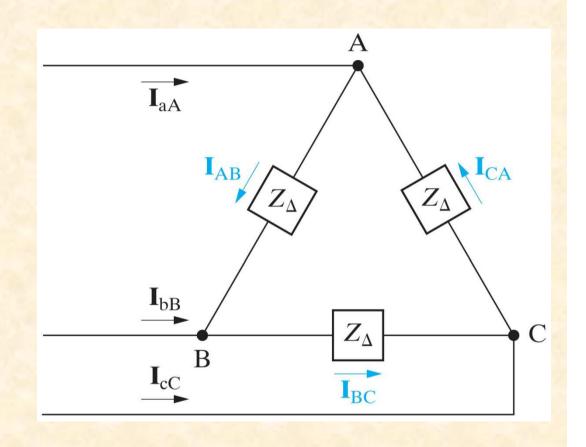
$$I_{CA} = \frac{V_{CA}}{Z_{\Delta}}$$

$$I_{AB} = I_{\phi} \angle 0^{\circ}$$

$$I_{BC} = I_{\phi} \angle -120^{\circ}$$

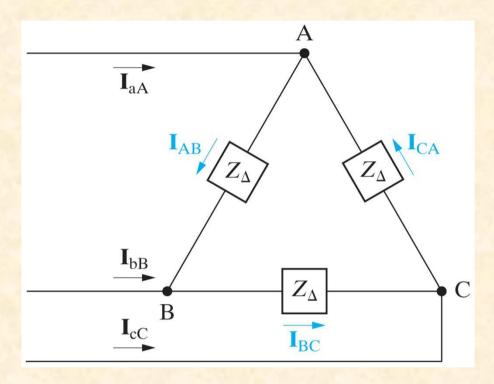
$$I_{CA} = I_{\phi} \angle 120^{\circ}$$

$$I_{CA} = I_{\phi} \angle 120^{\circ}$$





Balanced A-connected Load



$$I_{aA} = I_{AB} - I_{CA}$$

Line Currents

$$I_{_{bB}} = I_{BC} - I_{AB}$$

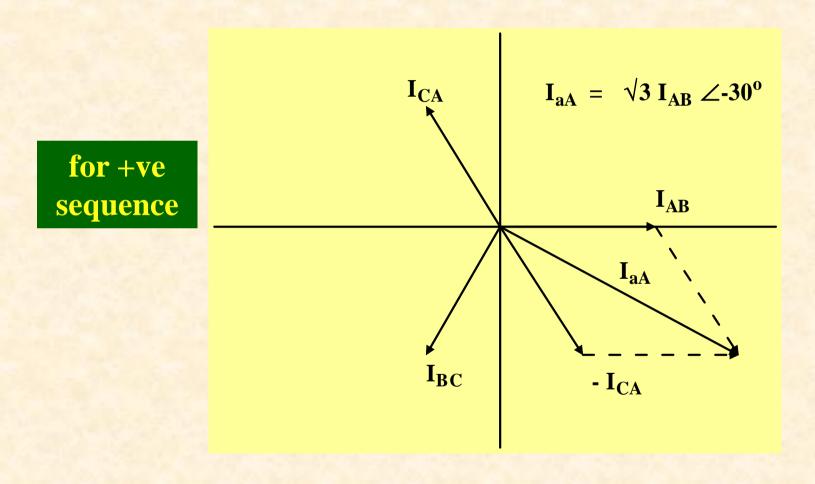
Phase Currents

$$I_{cC} = I_{CA} - I_{BC}$$





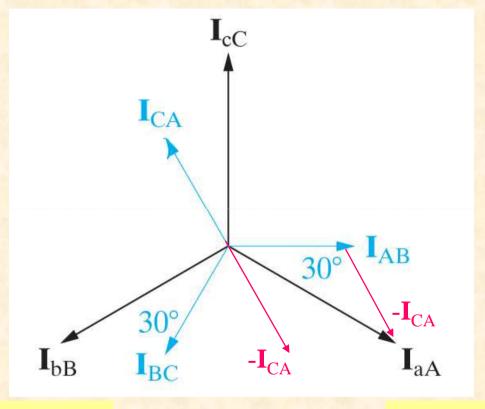
Line and Phase Currents for Balanced A-connected Load





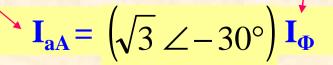
Line and Phase Currents for Balanced A-connected Load

for +ve sequence



 I_{aA} = Line Current

 I_{Φ} = Phase Current







Line and Phase Currents for Balanced A-connected Load

PHASE CURRENTS (I_b)

$$I_{aA} = I_{AB} - I_{CA}$$

$$I_{bB} = I_{BC} - I_{AB}$$

$$I_{cC} = I_{CA} - I_{BC}$$



$$I_{aA} = \sqrt{3} I_{AB} \angle -30^{\circ}$$

$$I_{bB} = I_{aA} \angle -120^{\circ}$$

$$I_{cC} = I_{aA} \angle + 120^{\circ}$$

LINE CURRENTS (I_L)

(for +ve sequence)



Conclusions for Balanced \(\Delta\-connected Load \)

The amplitude of the line current is equal to $\sqrt{3}$ times the phase current $\left|I_L\right| = \sqrt{3} \left|I_\phi\right|$

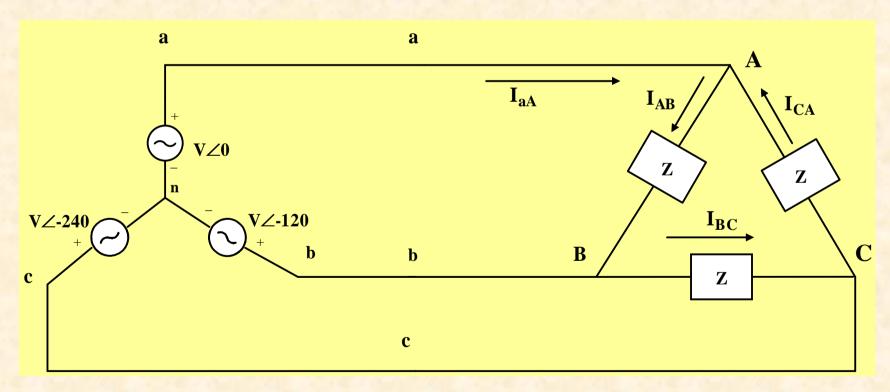
The set of line currents lags the phase currents by 30° (for +ve sequence) $\angle I_L = \angle I_\phi - 30^\circ$

The set of line currents leads the phase currents by 30° (for -ve sequence) $\angle I_L = \angle I_\phi + 30^\circ$



Balanced Y-A Three-Phase System

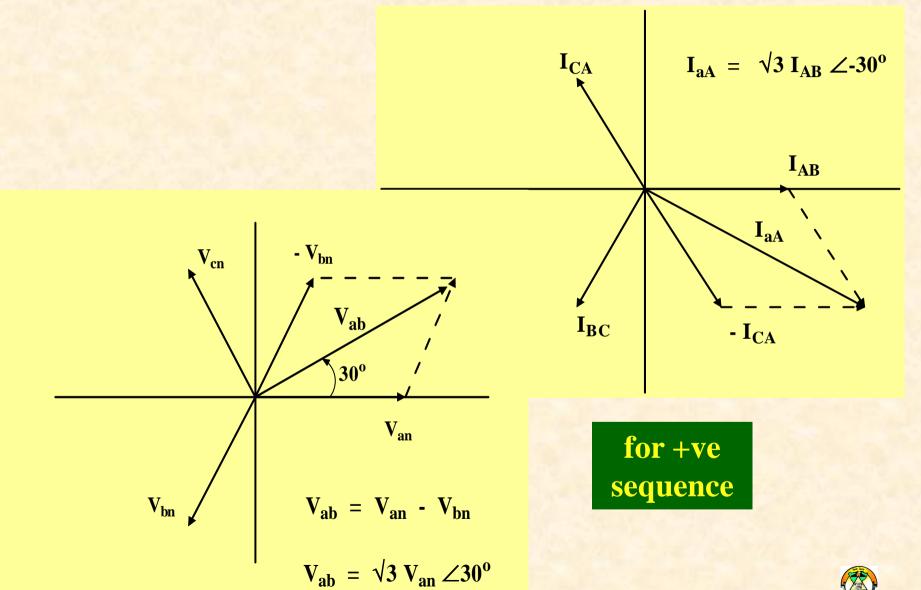
- Three phase sources are usually Y-connected and three phase loads are Delta connected.
- \triangleright There is no neutral connection for the Y- Δ system.







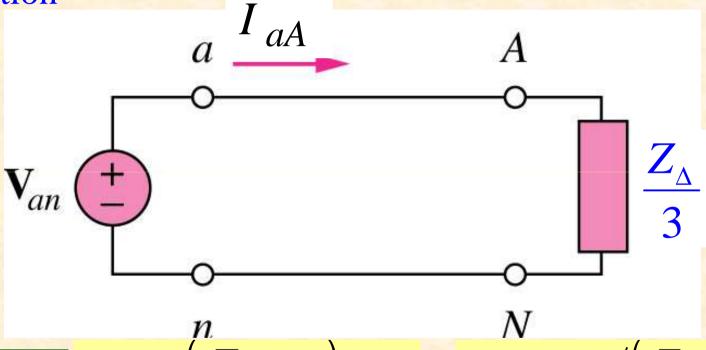
Balanced Y-A Three-Phase System





Balanced Y-A Three-Phase System

 \triangleright Single phase equivalent circuit of the balanced \mathbf{Y} - Δ connection



for +ve sequence
$$V_{AB} = (\sqrt{3} \angle 30^{o}) V_{AN} \& I_{AB} = I_{aA} / (\sqrt{3} \angle -30^{o})$$

for -ve sequence
$$V_{AB} = (\sqrt{3} \angle -30^{o}) V_{AN} \& I_{AB} = I_{aA} / (\sqrt{3} \angle 30^{o})$$





\triangleright Example on Y- \triangle System

The Y-connected source in Example 12.1 feeds a Δ -connected load through a distribution line having an impedance of $0.3 + j0.9 \Omega/\phi$. The load impedance is $118.5 + j85.8 \Omega/\phi$. Use the a-phase internal voltage of the generator as the reference.

- a) Construct a single-phase equivalent circuit of the three-phase 'system.
- b) Calculate the line currents I_{aA} , I_{bB} , and I_{cC} .
- c) Calculate the phase voltages at the load terminals.
- d) Calculate the phase currents of the load.

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e) Calculate the line voltages at the source terminals.



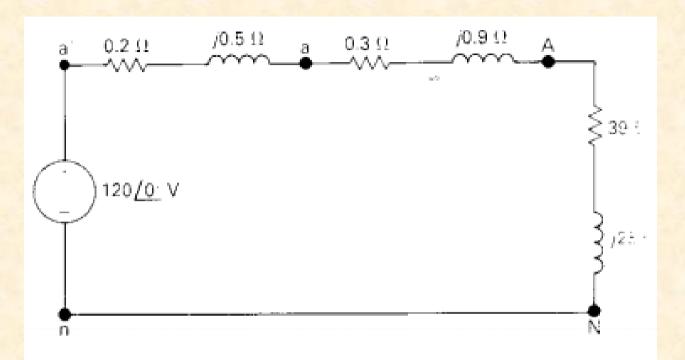


FIGURE 12.13 The single-phase equivalent circuit for Example 12.2.

 a) Figure 12.13 shows the single-phase equivalent circuit. The load impedance of the Y-equivalent is

$$\left(\frac{1}{3}\right)(118.5 + j85.8)$$
 or $39.5 + j28.6 \Omega/\phi$.



b) The a-phase line current is

$$\mathbf{I}_{aA} = \frac{120/0^{\circ}}{(0.2 + 0.3 + 39.5) + j(0.5 + 0.9 + 28.6)}$$
$$= \frac{120/0^{\circ}}{40 + j30} = 2.4/-36.87^{\circ} A.$$

Hence

$$I_{bB} = 2.4/-156.87^{\circ} A;$$

$$I_{cC} = 2.4/83.13^{\circ} A.$$



c) As the load is Δ -connected, the phase voltages are the same as the line voltages. To calculate the line voltages, we first calculate V_{AN} :

$$\mathbf{V}_{AN} = (39.5 + j28.6)(2.4/-36.87^{\circ})$$
$$= 117.04/-0.96^{\circ} \text{ V}.$$

Because the phase sequence is positive, the line voltage V_{AB} is

$$\mathbf{V}_{AB} = \sqrt{3/30^{\circ}} \mathbf{V}_{AN}$$

= 202.72/29.04° V.

Therefore

$$V_{BC} = 202.72 / -90.96^{\circ} V;$$

$$\mathbf{V}_{CA} = 202.72 / 149.04^{\circ} \, \text{V}.$$



d) The phase currents of the load may be calculated directly from the line currents:

$$I_{AB} = \frac{1}{\sqrt{3}} / 30^{\circ} I_{aA}$$

= 1.39/-6.87° A.

Once we know I_{AB} , we also know the other load phase currents:

$$I_{BC} = 1.39 / -126.87^{\circ} A;$$

 $I_{CA} = 1.39 / 113.13^{\circ} A.$

Note that we can check the calculation of I_{AB} by using the previously calculated V_{AB} and the impedance of the Δ -connected load. That is,

$$I_{AB} = \frac{V_{AB}}{Z_{\phi}} = \frac{202.72/29.04^{\circ}}{118.5 + j85.8}$$

= 1.39/-6.87° A.

(Alternative methods of calculation help eliminate errors, and we highly recommend their use in all work involving analysis and design.)



e) To calculate the line voltage at the terminals of the source, we first calculate V_{an} . Figure 12.13 shows that V_{an} is the voltage drop across the line impedance plus the load impedance, so

$$\mathbf{V}_{an} = (39.8 + j29.5)2.4 / -36.87^{\circ}$$

= $118.90 / -0.32^{\circ} \text{ V}.$

The line voltage V_{ab} is

$$V_{ab} = \sqrt{3/30^{\circ}} V_{an}$$
 or $V_{ab} = 205.94/29.68^{\circ} V$.

Therefore

$$V_{bc} = 205.94 / -90.32^{\circ} V;$$

 $V_{ca} = 205.94 / +149.68^{\circ} V.$



Common Source-Load Connection

- ✓ Common connection of source: Y
 - $-\Delta$ -connected sources: the circulating current may result in the delta mesh if the three phase voltages are slightly unbalanced.
- ✓ Common connection of load: △
 - Y-connected load: neutral line may not be accessible, load can not be added or removed easily.



Quiz No. (1)

✓ Calculate the line currents and line voltages at both load and source terminals

